## Exercise 2-5

There are now two "spots" in the server rather than one, shown in the table as two underlined spaces for In Service Arrival Times. Departure records are still placed on the event calendar, but we need to indicate in parentheses after the Arrival Times of entities in service their entity number to match them up with the correct departure records. Table 2-2 becomes:

| Just-Finished Event |  |  | Variables |  | Attributes | Statistical Accumulators |  |  |  |  |  |  |  |  | Event Calendar |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Entity <br> No. | Time <br> $t$ | Event <br> Type | $Q(t)$ | $B(t)$ | Arrival Times: <br> (In Queue) In Service | $P$ | $N$ | $\Sigma W Q$ | WQ* | $\Sigma T S$ | $T S^{*}$ | $\int Q$ | $Q^{*}$ | $\int B$ | [Entity | Time, | Type] |
| - | 0.00 | Init |  | 0 | () - | 0 | 0 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0 | 0.00 | $\begin{aligned} & {[1,} \\ & {[-,} \end{aligned}$ | $\begin{array}{r} 0.00 \\ 20.00 \end{array}$ | Arr] <br> End] |
| 1 | 0.00 | Arr | 0 | 1 | $\text { () } \frac{0.00(1)}{-}$ | 0 | 1 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0 | 0.00 | $\begin{aligned} & {[2,} \\ & {[1,} \\ & {[-,} \end{aligned}$ | $\begin{array}{r} 1.73 \\ 2.90 \\ 20.00 \end{array}$ | Arr] <br> Dep] <br> End] |
| 2 | 1.73 | Arr | 0 | 2 | $\text { () } \frac{0.00(1)}{\underline{1.73(2)}}$ | 0 | 2 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0 | 1.73 | $\begin{aligned} & {[1,} \\ & {[3,} \\ & {[2,} \\ & {[-,} \end{aligned}$ | $\begin{array}{r} 2.90, \\ 3.08, \\ 3.49 \\ 20.00 \\ \hline \end{array}$ | Dep] <br> Arr] <br> Dep] <br> End] |
| 1 | 2.90 | Dep | 0 | 1 | $\begin{array}{cc} () & - \\ \underline{1.73(2)} \end{array}$ | 1 | 2 | 0.00 | 0.00 | 2.90 | 2.90 | 0.00 | 0 | 4.07 | $\begin{aligned} & {[3,} \\ & {[2,} \\ & {[-,} \end{aligned}$ | $\begin{array}{r} 3.08 \\ 3.49 \\ 20.00 \end{array}$ | Arr] <br> Dep] <br> End] |
| 3 | 3.08 | Arr | 0 | 2 | $\text { () } \frac{3.08(3)}{1.73(2)}$ | 1 | 3 | 0.00 | 0.00 | 2.90 | 2.90 | 0.00 | 0 | 4.25 | [2, <br> [4, <br> [3, $[-$ | $\begin{array}{r} 3.49 \\ 3.79 \\ 6.47 \\ 20.00 \end{array}$ | Dep] <br> Arr] <br> Dep] <br> End] |
| 2 | 3.49 | Dep | 0 | 1 | $\text { () } \frac{3.08(3)}{-}$ | 2 | 3 | 0.00 | 0.00 | 4.66 | 2.90 | 0.00 | 0 | 5.07 | $\begin{aligned} & {[4,} \\ & {[3,} \\ & {[-,} \end{aligned}$ | $\begin{array}{r} 3.79 \\ 6.47, \\ 20.00, \end{array}$ | Arr] <br> Dep] <br> End] |
| 4 | 3.79 | Arr | 0 | 2 | $\text { () } \quad \begin{aligned} & 3.08(3) \\ & \underline{3.79(4)} \end{aligned}$ | 2 | 4 | 0.00 | 0.00 | 4.66 | 2.90 | 0.00 | 0 | 5.37 | $\begin{aligned} & {[5,} \\ & {[3,} \\ & {[4,} \\ & {[-,} \end{aligned}$ | $\begin{array}{r} \hline 4.41, \\ 6.47, \\ 8.31, \\ 20.00, \end{array}$ | $\begin{gathered} \text { Arr] } \\ \text { Dep] } \\ \text { Dep] } \\ \text { End] } \end{gathered}$ |
| 5 | 4.41 | Arr | 1 | 2 | $\begin{array}{ll} (4.41) & \underline{3.08(3)} \\ \hline \underline{3.79(4)} \end{array}$ | 2 | 4 | 0.00 | 0.00 | 4.66 | 2.90 | 0.00 | 1 | 6.61 | $\begin{aligned} & {[3,} \\ & {[4,} \\ & {[6,} \\ & {[-,} \end{aligned}$ | $\begin{array}{r} 6.47, \\ 8.31, \\ 18.69, \\ 20.00, \end{array}$ | Dep] <br> Dep] <br> Arr] <br> End] |
| 3 | 6.47 | Dep | 0 | 2 | $\text { () } \frac{4.41(5)}{\underline{3.79(4)}}$ | 3 | 5 | 2.06 | 2.06 | 8.05 | 3.39 | 2.06 | 1 | 10.73 | $\begin{aligned} & {[4,} \\ & {[5,} \\ & {[6,} \\ & {[-,} \end{aligned}$ | $\begin{array}{r} 8.31, \\ 10.93, \\ 18.69, \\ 20.00, \\ \hline \end{array}$ | $\begin{gathered} \text { Dep] } \\ \text { Dep] } \\ \text { Arr] } \\ \text { End] } \end{gathered}$ |
| 4 | 8.31 | Dep | 0 | 1 | $\text { () } \frac{4.41(5)}{-}$ | 4 | 5 | 2.06 | 2.06 | 12.57 | 4.52 | 2.06 | 1 | 14.41 | $\begin{aligned} & {[5,} \\ & {[6,} \\ & {[-,} \end{aligned}$ | $\begin{aligned} & 10.93 \\ & 18.69 \\ & 20.00 \end{aligned}$ | Dep] <br> Arr] <br> End] |
| 5 | 10.93 | Dep | 0 | 0 | $\begin{array}{ll} \text { () } & - \\ & - \end{array}$ | 5 | 5 | 2.06 | 2.06 | 19.09 | 6.52 | 2.06 | 1 | 17.03 | $\begin{aligned} & {[6,} \\ & {[-,} \end{aligned}$ | $\begin{aligned} & 18.69 \\ & 20.00 \end{aligned}$ | Arr] <br> End] |
| 6 | 18.69 | Arr | 0 | 1 | $\text { () } \frac{18.69(6)}{-}$ | 5 | 6 | 2.06 | 2.06 | 19.09 | 6.52 | 2.06 | 1 | 17.03 | $\begin{aligned} & {[7,} \\ & {[-,} \\ & {[6,} \end{aligned}$ | $\begin{aligned} & 19.39 \\ & 20.00 \\ & 23.05 \end{aligned}$ | Arr] <br> End] <br> Dep] |
| 7 | 19.39 | Arr | 0 | 2 | $\text { () } \frac{18.69(6)}{\underline{19.39(7)}}$ | 5 | 7 | 2.06 | 2.06 | 19.09 | 6.52 | 2.06 | 1 | 17.73 | $\begin{aligned} & {[-,} \\ & {[7,} \\ & {[6,} \\ & {[8,} \end{aligned}$ | $\begin{aligned} & 20.00, \\ & 21.46, \\ & 23.05, \\ & 34.91, \end{aligned}$ | End] <br> Dep] <br> Dep] <br> Arr |
| - | 20.00 | End | 0 | 2 | $\text { () } \frac{18.69(6)}{\underline{19.39(7)}}$ | 5 | 7 | 2.06 | 2.06 | 19.09 | 6.52 | 2.06 | 1 | 18.95 | $\begin{aligned} & {[7,} \\ & {[6,} \\ & {[8,} \end{aligned}$ | $\begin{aligned} & 21.46, \\ & 23.05, \\ & 34.91, \end{aligned}$ | Dep] <br> Dep] <br> Arr] |

Here are the summary results:

| Performance <br> Measure | Value | Result from Table 2-3 | Change |
| :--- | :--- | :--- | :--- |
| Total <br> production | 5 parts | 5 parts | No change |
| Average waiting time <br> in queue | 0.29 minute per part <br> $(7$ parts) | 2.53 minutes per part <br> $(6$ parts $)$ | Decreased |
| Maximum waiting <br> time in queue | 2.06 minutes | 8.16 minutes | Decreased |
| Average total time in <br> system | 3.82 minutes per part <br> $(5$ parts $)$ | 6.44 minutes per part <br> $(5$ parts $)$ | Decreased |
| Maximum total time <br> in system | 6.52 minutes | 12.62 minutes | Decreased |
| Time-average number <br> of parts in queue | 0.10 part | 0.79 part | Decreased |
| Maximum number of <br> parts in queue | 1 part | 3 parts | Decreased |
| Drill-press utilization | $0.47[=18.95 /(2 \times 20)]$ <br> $($ dimensionless proportion $)$ | 0.92 <br> $($ dimensionless proportion) |  |

Congestion is considerably relieved on all measures; the average total time in system is reduced the least since parts must still endure their (same) processing times no matter how little time they have to wait in queue.

