



Computer Security

Message Authentication Codes,
Hashes and Message Digests

What Problems are We Trying to Solve?

- **Authentication**

- The process of reliably verifying the identity of someone or something
 - In particular, did a message indeed come from its specified sender?

- **Need to guard against:**

- Disclosure of a message to any unauthorized person or system
- Messages masquerading as being from a source
- Content modification
 - Was the message changed between sender and recipient?)
- Source or destination repudiation
 - Can the sender or recipient deny they sent/received the message?

Authentication Functions

- Three main classes:

- **Message Encryption**

- Ciphertext of entire message serves as its authenticator

- **Message Authentication Code (MAC)**

- Function of the message and a secret key which produces a fixed-length authenticator value

- **Hash Function**

- Function which maps a message of any length into a fixed-size hash authenticator value

Message Encryption

- We've already seen various encryption options:

- **Symmetric Encryption** – provides both *confidentiality* and *authentication*

- **Public Key Encryption:**

$$C = E_{KU_b}(P) ; P = D_{KR_b}(C) \quad \triangleright \text{provides } \textit{confidentiality} \text{ only}$$

$$C = E_{KR_b}(P) ; P = D_{KU_b}(C) \quad \triangleright \text{provides } \textit{authentication \& signature}$$

$$C = E_{KU_a}(E_{KR_b}(P)) \quad \triangleright \text{provides } \textit{confidentiality, authentication, and signature}$$
$$P = D_{KR_a}(D_{KU_b}(C))$$

Message Authentication Code (MAC)

- Uses a secret key to generate a small fixed-size block of data: a **Cryptographic Checksum**, or **MAC**
- If Alice and Bob share a common secret key, K , then:

$$MAC = F_K(P)$$

where:

P is the input plaintext

F is the MAC function

K is the shared secret key

MAC is the resulting message authentication code

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Message Authentication Code (MAC)

- The MAC is sent to the recipient along with its associated message
 - The recipient uses the same MAC function and key on the message and compares the result with the transmitted MAC.
 - If the two MACs match, the recipient is assured that:
 - The message has not been altered, and
 - The message is from the alleged sender
 - If the message contains a sequence number (e.g. TCP header), then the recipient is assured of the proper sequencing of messages

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Message Authentication Code (MAC)

- A MAC function is similar to an encryption function, except that the MAC function **need not be reversible**.
- A MAC function is typically a **many-to-one function**:
 - The input messages can be of any length, but
 - The output is of fixed length (n bits)
- If an n -bit MAC function (that is, a MAC function that generates a fixed-size n -bit block) is used, how many possible MAC values are there?

$$2^n$$

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Message Authentication Code (MAC)

- For example, assume:
 - We are using a 10-bit MAC function
 - We are using 100-bit messages
 - There are:
 - 2^{100} ($\sim 1.27 * 10^{30}$) different possible messages:
 - only 2^{10} (1024) different possible MACs
- so, on average, each MAC value is generated by a total of

$$\frac{2^{100}}{2^{10}} = 2^{90} \approx 1.24 \times 10^{27}$$

different messages

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Message Authentication Code (MAC)

- Here are some basic uses of MACs:

P = Plaintext
 C = Ciphertext
 E = Encryption function
 F = MAC function
 K = Key
 M = Message sent

$$M = P \parallel F_K(P)$$

- Plaintext concatenated with MAC
- Provides **authentication** only

$$M = E_{K_2}(P \parallel F_{K_1}(P))$$

- Symmetric key encrypted ciphertext concatenated with plaintext MAC
- Provides **authentication** and **confidentiality**
- Authentication tied to plaintext

$$C = E_{K_2}(P) ; M = C \parallel F_{K_1}(C)$$

- Symmetric key encrypted ciphertext concatenated with ciphertext MAC
- Provides **authentication** and **confidentiality**
- Authentication tied to ciphertext

Message Authentication Code (MAC)

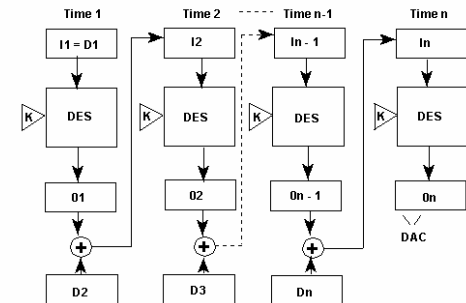
- Why use MACs for authentication, instead of symmetric encryption?
 - Performance – MAC functions are faster than encryption functions
 - Some applications don't care about secrecy/confidentiality, but care a lot about authentication (e.g. SNMP)
 - Separation of authentication and confidentiality provides greater flexibility.
 - Certain applications may wish to prolong the period of authentication so that a message can undergo several phases of processing which rely on that authentication.
 - As soon as the message is decrypted, the message is no longer protected against modification
 - A MAC can be kept with the message to retain this protection.

Message Authentication Code (MAC)

- One of the most widely used MACs is the **Data Authentication Algorithm (DAA)**, based on on DES
 - DAA is both a FIPS publication (FIPS PUB 113*) and an ANSI standard (X9.17)
 - It uses the Cipher Block Chaining (CBC) mode of operation with an initialization vector of zero.
 - The data are grouped into contiguous 64-bit blocks; if necessary, the final block is padded on the right with zeroes to form a full 64-bit block.
 - Using the DES encryption algorithm, E , and a secret key, K , a **Data Authentication Code (DAC)** is calculated...

*<http://www.itl.nist.gov/fipspubs/fip113.htm>

Digital Authentication Algorithm



D = Data Block K = DES Key
 I = Input Block O = Output Block
 DES = Data Encryption Standard $(+)$ = Exclusive-OR

One-Way Hash Functions

- Can be viewed as a variation on a MAC function:
 - A **Hash Function** accepts a variable-size message, M , as input and produces a fixed-size output, referred to as a **Hash Code**, or **Message Digest**:
$$h = H(M)$$
 - Unlike a MAC function, a hash code:
 - *does not use a key*, and so
 - *is a function only of the input message*
 - A change to any bit (or bits) of the message results in a change to the hash code, which can provide an **error-detection capability**.
 - A message digest can be used as a **fingerprint** for a message, to allow detection of message modification

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One-Way Hash Functions

- Requirements for a hash function are:
 - Can be applied to a block of data of any size
 - Produces a fixed-length output
 - $H(M)$ is relatively easy to compute for any given M , allowing for both software and hardware implementations
 - For any given value h , it is computationally infeasible to find M such that $h = H(M)$. This is the **One-way Property**.
 - For any given block, M , it is computationally infeasible to find $M' \neq M$ with $H(M') = H(M)$.
 - This is called **Weak Collision Resistance**.
 - It is computationally infeasible to find any pair (M, M') such that $H(M) = H(M')$.
 - This is called **Strong Collision Resistance**.

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One-Way Hash Functions

- Here are some basic uses of hash functions:

$$M = E_K(P \| H(P))$$

- Provides confidentiality and authentication

$$M = P \| E_K(H(P))$$

- Provides authentication (amounts to a MAC)

$$M = P \| E_{KR_a}(H(P))$$

- Provides authentication
- Also provides a digital signature (because only the sender could have produced the encrypted hash code)

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One-Way Hash Functions

- ...and some more:

$$M = E_K(P \| E_{KR_a} H(P))$$

- Provides confidentiality, authentication and digital signature

$$M = P \| H(P \| S)$$

- Provides authentication, using a shared secret, S

$$M = E_K(P \| H(P \| S))$$

- Adds confidentiality to the above mechanism.

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One-Way Hash Functions

- The drive for hash/message digest algorithms began with public key cryptography
 - RSA was invented, but it was slow enough at that time to make it impractical when used alone.
 - A cryptographically secure message digest algorithm with high performance would make RSA much more useful.

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One-Way Hash Functions

- Thus, **MD** (unpublished) and **MD2** (defined in RFC 1319¹) were invented by Ron Rivest (of RSA fame)
 - MD2 is a 128-bit one-way hash function
- Ralph Merkle (of Xerox at the time, but who had worked at Stanford with Diffie & Hellman) came up with a message digest algorithm called **SNEFRU**²
 - It was several times faster than MD2
 - It is a 128-bit or 256-bit one-way hash function
- This prompted Rivest to respond with **MD4** (defined in RFC 1320³)
 - MD4 produces a 128-bit hash

¹<http://www.faqs.org/rfcs/rfc1319.html>

²[Snefru was an Egyptian Pharaoh](#)

³<http://www.faqs.org/rfcs/rfc1320.html>

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One-Way Hash Functions

- Weaknesses were found in the MD4 algorithm, so Rivest came up with **MD5** (defined in RFC 1321¹)
 - MD5 is similar to MD4, but improved.
 - More complex than MD4, but similar in design
 - Also produces a 128-bit hash

¹<http://www.faqs.org/rfcs/rfc1321.html>

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One-Way Hash Functions

- The NSA designed the **Secure Hash Algorithm (SHA)**
- The National Institute of Standards and Technology (NIST), made it a standard.
 - They revised it very late in the game, because of some (unspecified) weakness that had been found, and changed its name to **SHA-1**¹.
 - SHA-1 is a 160-bit hash function based on MD4
 - Shares much in common with MD5, but has a much more conservative design.
 - 2 or 3 times slower than MD5

¹<http://www.itl.nist.gov/fipspubs/fip180-1.htm>

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One-Way Hash Functions

- Because of improving computing environments, the 160-bit hash of SHA-1 is now becoming a liability
- So NIST produced *SHA-256*, *SHA-384*, and *SHA-512*¹.
 - Designed to be used with the 128-, 192- and 256-bit key sizes of AES.
 - Structure similar to SHA-1, but much slower.
 - According to Ferguson & Schneier, they are too new to have experienced significant cryptanalysis attacks, and so are not yet proven. But they also say that MD5 and SHA-1 are not sufficiently secure, so you may have little choice.

<http://csrc.nist.gov/publications/fips/fips180-2/fips180-2.pdf>

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Typical Usage of Digests

- Here's an example of the use of SHA-1 in a real application – Java JAR files:
 - In the `jce.jar` (Java Cryptography Extension) JAR file, the *manifest* contains the following:

```
Manifest-Version: 1.0
Created-By: 1.4.1-internal (Sun Microsystems Inc.)

Name: javax/crypto/SealedObject.class
SHA1-Digest: R+GWl6Zuqgtty1zOaP5RrRSgfQo=

Name: javax/crypto/KeyAgreementSpi.class
SHA1-Digest: fdmlqpiTRMzV65+9304tJ3Uo6wg=

Name: javax/crypto/spec/DESedeKeySpec.class
SHA1-Digest: Q7UJvLuk8GST42GW6xD1XHe3Xv8=

Name: javax/crypto/spec/DHParameterSpec.class
SHA1-Digest: y0oY9yd/BQQxEc/2q1Cytta/r2E=

Name: javax/crypto/interfaces/DHPrivateKey.class
SHA1-Digest: jwgw7pakTyK0LBNivsp6V6Ad4k=

...
```

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One-Way Hash Functions

- Ferguson & Schneier¹ recommend the following:
 - They don't feel that any of the existing hash functions is sufficiently secure when used as is.
 - So, they define a double hash function, $h_d = h(h(m))$
 - They recommend the use of SHA_d-256 , or, for higher security levels, SHA_d-512

¹ *Practical Cryptography*, by Niels Ferguson and Bruce Schneier, Wiley.

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HMAC

- HMAC¹ is an attempt to use a hash function to build a MAC.
- Note that:
 - Hash functions provide only $n/2$ bits of security against some attacks
 - A MAC function is expected to provide n bits of security.
 - Defining:
 $MAC(K, m) = h(K || m)$, or $h(m || K)$, or $h(K || m || K)$
is not secure if you use one of the standard hash functions.
- HMAC was proven to be secure if the underlying hash function's underlying compression function was secure.

¹<http://www.faqs.org/rfcs/rfc2104.html>

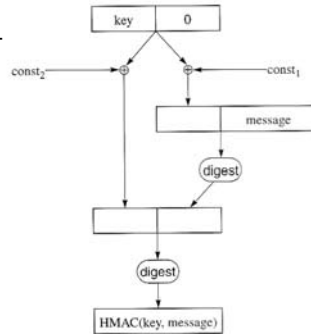
There is also a draft FIPS at:

<http://csrc.nist.gov/CryptoToolkit/hmac/fr-hmac-200101.html>

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HMAC

- HMAC takes a variable length key and a variable length message, and produces a fixed-size output that is the same size as the underlying hash function.
 - It first pads the key with 0 bits to 512 bits
 - If the key is larger than 512 bits, it first hashes the key, resulting in 128 or 160 bits, and then pads the result out to 512 bits.
 - It then XORs the padded key with a constant string of octets of value 36 (hex), then concatenates the result with the message, and computes a hash (digest)
 - It XORs the padded key with a different constant string of octets of value 5C (hex), concatenates that with the result of the of the first hash, and computes a second hash on that.



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HMAC

- Examples of HMAC algorithms are:
 - HmacMD5 – uses the MD5 hash algorithm
 - HmacSHA1 – uses the SHA-1 hash algorithm

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Summary

- We've covered:
 - A little about authentication
 - Somewhat more about Message Authentication Codes (MACs)
 - Even more about One-Way Hash Functions (also known as Message Digests or Message Digest Functions)
- We have also seen how they are all related to previous cryptography topics

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